|     | Λ |   | Λ |
|-----|---|---|---|
| For | A | W | A |

Name Class

# GCSE Mathematics Specification

Paper 3 Foundation Tier

Churchill Paper 3E

1 hour 30 minutes

### **Materials**

### For this paper you must have:

- · a calculator
- · mathematical instruments



### Instructions

- Use black ink or black ball-point pen.
- · Draw diagrams in pencil.
- Write your name and class in the box at the top of the page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- In all calculations, show clearly how you work out your answer.

## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.



Written by Shaun Armstrong

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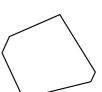
# Answer all questions in the spaces provided.

1 Which of these shapes is **not** a hexagon?

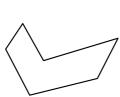
Circle the correct letter.

[1 mark]

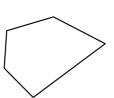
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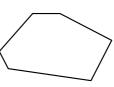
В



C



D



2 Which of these numbers is a square number **and** a cube number?

Circle your answer.

[1 mark]

8

16

64

81

3 How many of these fractions are **larger** than  $\frac{2}{3}$ ?

1/2

11 15 <u>5</u>

Circle your answer.

[1 mark]

0

1

2

3

| 4 | A ba | ag contains 6 p                   | ink balls and 8 gre                    | een balls.                    |                          |                   |
|---|------|-----------------------------------|--|-------------------------------|--------------------------|-------------------|
|   |      | k out the small<br>to green balls |  | ls you can remo               | ve from the bag so that  | the ratio of pink |
|   | Circ | le your answer                    |  |                               |                          | [1 mark]          |
|   |      | 2                                 | 3                                      | 5                             | 7                        | [ i iliai k]      |
|   |      | 2                                 | 3                                      | 3                             | ,                        |                   |
|   |      |                                   |  |                               |                          |                   |
|   |      |                                   |  |                               |                          |                   |
|   |      |                                   |  |                               |                          |                   |
|   |      |                                   |  |                               |                          |                   |
|   |      |                                   |  |                               |                          |                   |
|   |      |                                   |  |                               |                          |                   |
| 5 | (a)  | 0                                 | s in a pot are gold                    |                               |                          |                   |
|   |      | The rest of th                    | e coins in the pot                     | are silver-colou              | red.                     |                   |
|   |      | Write down tl                     | ne ratio of gold-co                    | loured to silver-             | coloured coins in the po | ot.<br>[1 mark]   |
|   |      |                                   |  |                               |                          |                   |
|   |      |                                   |  |                               |                          |                   |
|   |      |                                   | Ansv                                   | wer                           | :                        |                   |
| 5 | (b)  | 35% of the bo                     | ottles in a wine radie bottles contain | ck contain white<br>red wine. | wine.                    |                   |
|   |      |                                   |  |                               | bottles in the rack.     |                   |
|   |      | Give your rat                     | io in its simplest fo                  | OIIII.                        |                          | [2 marks]         |
|   |      |                                   |  |                               |                          |                   |
|   |      |                                   |  |                               |                          |                   |
|   |      |                                   |  |                               |                          |                   |
|   |      |                                   | Ane                                    | wor                           | :                        |                   |
|   |      |                                   | Alls                                   | wei                           | ·                        |                   |
|   |      |                                   |  |                               |                          |                   |
|   |      |                                   |  |                               |                          |                   |

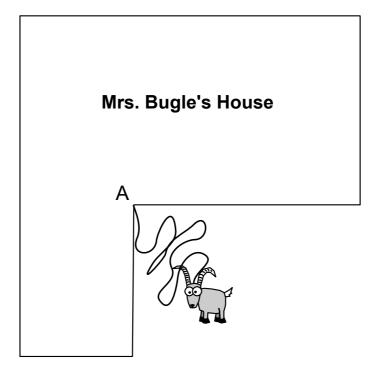
| 6 | (a) | Solve 5 <i>m</i> = 12     | [1 mark]  |
|---|-----|---------------------------|-----------|
| 6 | (b) | AnswerSimplify $5y-2+y+3$ | [2 marks] |
| 6 | (c) | Answer                    |           |
| 6 | (d) | Answer                    | [2 marks] |
|   |     | Answer                    |           |

| Normal b                            | ouquet        | £27   |
|-------------------------------------|---------------|---|
| Special b                           |               | £45   |
| Corsage                             | -             | £3.50   |
| Table arr                           | angement      | £12   |
| 10% discount w                      | hen you spe   | end over £400                                       |
| Louisa plans to order arrangements. | r 6 normal bo | ouquets, 2 special bouquets, 9 corsages and 8 table |
| Fatat says                          |               |   |
| "If you order or                    | ne extra norn | nal bouquet you'll pay less in total."              |
| Is Fatat correct?                   |               |   |
| You must justify your               | answer.       | [5 mark   |
|                                     |               | [5 mark   |
|                                     |               |   |
|                                     |               |   |
|                                     |               |   |
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|                                     |               |   |
|                                     |               | Answer  |
|                                     |               | Answer  |
|                                     | ,             | Answer  |
|                                     |               | Answer  |

| 8 | Mike       | e has two c                | lice with coloured sides                             | i.  |                                    |
|---|------------|----------------------------|--|---|------------------------------------|
|   | The<br>The | first dice h<br>second did | as 2 red sides, 2 yellov<br>ce has 1 blue side, 2 gr | v sides and 2 white sides.<br>een sides and 3 purple sides. | des.                               |
|   | Mike       | e rolls the t              | wo dice.   |   |                                    |
| 8 | (a)        | List all th                | e possible outcomes.                                 |   |                                    |
|   |            | One has                    | been done for you.                                   |   |                                    |
|   |            |                            |  |   | [2 marks]                          |
|   |            |                            | First Dice   | Second Dice   |                                    |
|   |            |                            | Red  | Blue  |                                    |
|   |            |                            |  |   |                                    |
|   |            |                            |  |   |                                    |
|   |            |                            |  |   |                                    |
|   |            |                            |  |   |                                    |
|   |            |                            |  |   |                                    |
|   |            |                            |  |   |                                    |
|   |            |                            |  |   |                                    |
|   | Cim        | 000 0010                   |  |   |                                    |
|   | SIIII      | one says                   | de anno a frailine and an                            | the first disc and blue as                                  | 45                                 |
| _ | 41.        |                            |  | the first dice and blue on                                  | the second dice is $\frac{1}{9}$ . |
| 8 | (b)        | Explain v                  | why Simone is wrong.                                 |   | [1 mark]                           |
|   |            |                            |  |   |                                    |
|   |            |                            |  |   |                                    |
|   |            |                            |  |   |                                    |
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|   |            |                            |  |   |                                    |

9 5 Speed (m/s) 4 3 2 1 0 5 0 10 15 Time (minutes) The graph shows Will's speed during and just after a race. 9 What was Will's highest speed during the race. [1 mark] Answer \_\_\_\_\_ m/s 9 **(b)** Work out how far Will ran during the 5th minute of the race. [2 marks] Answer 9 After how many minutes did Will finish the race? (c) Explain how you can tell this from the graph. [2 marks] minutes

| 10 | (a) | Use your calculator to work out   |           |
|----|-----|---|-----------|
|    |     | $\frac{3.2 \times 4.9}{3 - \sqrt{6}}$                                     |           |
|    |     | giving your answer correct to 1 decimal place.                            | [2 marks] |
|    |     |   |           |
|    |     | Answer  |           |
| 10 | (b) | Using your calculator, find the values of x and y such that               |           |
|    |     | $6860 = 2^x \times 5 \times 7^y$  | [2 marks] |
|    |     |   |           |
|    |     |   |           |
|    |     | x =   |           |
|    |     | <i>y</i> =  |           |
| 10 | (c) | Hence, or otherwise, find the Highest Common Factor (HCF) of 294 and 6860 |           |
|    |     |   | [2 marks] |
|    |     |   |           |
|    |     |   |           |
|    |     | Answer  |           |



Scale: 1:100

The map shows Mrs Bugle's house using a scale of 1:100

Mrs. Bugle owns a goat called Billy.

There is grass all around the house which Billy likes to graze on.

However, he is tethered to the corner of the house labelled A by a 10 metre long rope.

Construct the region of grass that Billy is able to reach.

[4 marks]

Rosa looked at the 30 houses for sale in the window of an estate agents. This table shows how many bedrooms each one had.

| Number of bedrooms | Frequency |
|--------------------|-----------|
| 1                  | 2         |
| 2                  | 9         |
| 3                  | 12        |
| 4                  | 5         |
| 5                  | 2         |

| 12 | (a) | Calculate the mean number of bedrooms in these houses.                     | [3 marks] |
|----|-----|--|-----------|
|    |     |  |           |
|    |     |  |           |
|    |     |  |           |
|    |     |  |           |
|    |     |  |           |
|    |     |  |           |
|    |     |  |           |
|    |     | Answer   |           |
|    | The | estate agents have another 318 houses for sale.                            |           |
| 12 | (b) | Calculate an estimate for the number of these houses that have 4 bedrooms. | [2 marks] |
|    |     |  |           |
|    |     | Answer   |           |
|    |     |  |           |
| 12 | (c) | State an assumption you have made in your calculation in part (b).         | [1 mark]  |
|    |     |  |           |
|    |     |  |           |
|    |     |  |           |
|    |     |  |           |

| 13 | Here | are the ingredients f  | or a recipe to   | make 30 c       | ookies.             |                       |
|----|------|--|--|-----------------|---------------------|-----------------------|
|    |      | 225 g butter<br>110 g caster suga<br>270 g plain flour<br>85 g chocolate ch          |  |                 |                     |                       |
| 13 | (a)  | Circle the weight of   | the raw ingred   | dients in on    | e cookie.           | [1 mark]              |
|    |      | 15g  | 17g  | 19g             | 23g                 |                       |
| 13 | (b)  | Jack has 180 g of pl   | -  | •               | -                   |                       |
|    |      | 15   | 18   | 20              | 24                  | [1 mark]              |
|    | Here | e are the prices for the<br>Butter<br>Caster sugar<br>Plain flour<br>Chocolate chips | 85 p for 25<br>£2.45 for 2<br>£1 for 1.51<br>80 p for 10 | 0g<br>≧kg<br>kg | l's local supermark | et.                   |
| 13 | (c)  | ingredients that she   | buys.  |                 |                     | ever waste any of the |
|    |      | Work out how much Give your answer in  | -  |                 |                     | makes.                |
|    |      |  |  |                 |                     | [3 marks]             |
|    |      |  |  |                 |                     |                       |
|    |      |  |  |                 |                     |                       |
|    |      |  | Answer _   |                 |                     | pence                 |

| 14 | A ni | ece of wire is in the shape of a circle of diameter 10.2 cm.                    |
|----|------|---|
| 14 | ∠ hι | see of whe is in the shape of a choic of diameter 10.2 cm.                      |
|    |      | Not drawn accurately  |
|    | The  | wire is straightened and then formed into the shape of an equilateral triangle. |
|    |      | Not drawn accurately  |
| 14 | (a)  | Work out the side length of the triangle.                                       |
|    |      |   |
|    |      | [3 marks]   |
|    |      | Answer cm   |
|    |      |   |
|    |      |   |
|    |      |   |

|    | Next   | the wire is forme | ed into the shape of a  | square.<br>drawn accurately |                 |                 |
|----|--------|-------------------|---|-----------------------------|-----------------|-----------------|
| 14 | (b)    | Work out the ar   | ea of the square.   |                             |                 | [2 marks]       |
|    |        |                   |   |                             |                 |                 |
|    |        |                   |   |                             |                 |                 |
|    |        |                   |   |                             |                 |                 |
|    |        |                   |   |                             |                 |                 |
|    |        |                   |   |                             |                 |                 |
|    |        |                   | Answer _  |                             |                 | cm <sup>2</sup> |
| 15 | 75%    | of the dogs that  | at visit a pet groomin<br>visit come back within<br>nals that visit come ba | n one month.                | 1.              |                 |
|    | Circle | e the percentage  | of all the animals tha  | it visit the salon that     | come back withi | n one month.    |
|    |        | 55.50/            | 04.50/  | 05.5%                       | 07.5%           | [1 mark]        |
|    |        | 55.5%             | 64.5%   | 65.5%                       | 67.5%           |                 |
|    |        |                   |   |                             |                 |                 |
|    |        |                   |   |                             |                 |                 |
|    |        |                   |   |                             |                 |                 |
|    |        |                   |   |                             |                 |                 |
|    |        |                   |   |                             |                 |                 |

| 6 | Bobby is playing with plastic rectangles.  Each rectangle measures 6 cm by 4 cm.   |
|---|--|
|   | He takes 5 of the rectangles and arranges them into a larger rectangle like this.  |
|   | Not drawn accurately   |
|   | Bobby then moves two of the rectangles to make a different large rectangle like this.  |
|   |  |
|   |  |
|   | The two larger rectangles have different perimeters.   |
|   | Work out the percentage change in the perimeter as a result of the change Bobby made.  |
|   | Work out the percentage change in the perimeter as a result of the change Bobby made.  State clearly whether the change is an increase or decrease.  [3 marks] |
|   | State clearly whether the change is an increase or decrease.   |
|   | State clearly whether the change is an increase or decrease.   |
|   | State clearly whether the change is an increase or decrease.   |
|   | State clearly whether the change is an increase or decrease.   |
|   | State clearly whether the change is an increase or decrease.   |
|   | State clearly whether the change is an increase or decrease.   |
|   | State clearly whether the change is an increase or decrease.   |

| 17  | Circle the area that is the same as 20 cm <sup>2</sup>                     |                      |                      |                       | [1 mark]  |
|-----|--|----------------------|----------------------|-----------------------|-----------|
|     | 0.2 m <sup>2</sup>   | 0.02 m <sup>2</sup>  | 0.002 m <sup>2</sup> | 0.0002 m <sup>2</sup> |           |
|     |  |                      |                      |                       |           |
|     |  |                      |                      |                       |           |
|     |  |                      |                      |                       |           |
|     |  |                      |                      |                       |           |
|     |  |                      |                      |                       |           |
| 18  | 75 students from Year  | 10 and Year 11 o     | go on a camping tr   | p.                    |           |
| - • | 33 of the students are<br>37 of the students are<br>13 of the students are | in Year 11.<br>boys. |                      | ,                     |           |
|     | One of the students is   | er.                  |                      |                       |           |
|     |  |                      |                      |                       |           |
|     | Work out the probabili   | y that the student   | t is a Year 10 girl. |                       | [3 marks] |
|     | Work out the probability   | y that the studen    | t is a Year 10 girl. |                       | [3 marks] |
|     | Work out the probability   | y that the studen    | t is a Year 10 girl. |                       | [3 marks] |
|     | Work out the probability   | y that the studen    | t is a Year 10 girl. |                       | [3 marks] |
|     | Work out the probability   | y that the studen    | t is a Year 10 girl. |                       | [3 marks] |
|     | Work out the probability   | y that the student   | t is a Year 10 girl. |                       | [3 marks] |
|     | Work out the probability   | y that the student   | t is a Year 10 girl. |                       | [3 marks] |
|     | Work out the probability   | y that the student   | t is a Year 10 girl. |                       | [3 marks] |
|     | Work out the probability   | Answer               |                      |                       | [3 marks] |
|     | Work out the probability   |                      |                      |                       | [3 marks] |

| 19 | Thre  | Three friends, Ayyub, Bran and Curtis, each have some mini chocolate eggs.                 |           |  |  |  |  |  |
|----|---|--|-----------|--|--|--|--|--|
|    | Bran has 1 more egg than Ayyub. Curtis has 50% more eggs than Bran. |  |           |  |  |  |  |  |
|    | Altogether, Ayyub, Bran and Curtis have 48 chocolate eggs.          |  |           |  |  |  |  |  |
|    |   |  |           |  |  |  |  |  |
|    |   | Curtis gives eggs to each of Ayyub and Bran so that they all have the same number of eggs. |           |  |  |  |  |  |
|    | Wor   | k out how many eggs Curtis gives away in total.  | [4 marks] |  |  |  |  |  |
|    |   |  |           |  |  |  |  |  |
|    |   |  |           |  |  |  |  |  |
|    |   |  |           |  |  |  |  |  |
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|    |   |  |           |  |  |  |  |  |
|    |   | Answer   | _         |  |  |  |  |  |
| 20 | (a)   | Factorise $p^2 - 16$   | [2 marks] |  |  |  |  |  |
|    |   | Answer   |           |  |  |  |  |  |
| 20 | (b)   | Solve $t^2 + 2t - 8 = 0$   | [3 marks] |  |  |  |  |  |
|    |   |  |           |  |  |  |  |  |
|    |   |  |           |  |  |  |  |  |
|    |   | Answer   |           |  |  |  |  |  |

21 250 people entered a theme park while Joan was on the gate.

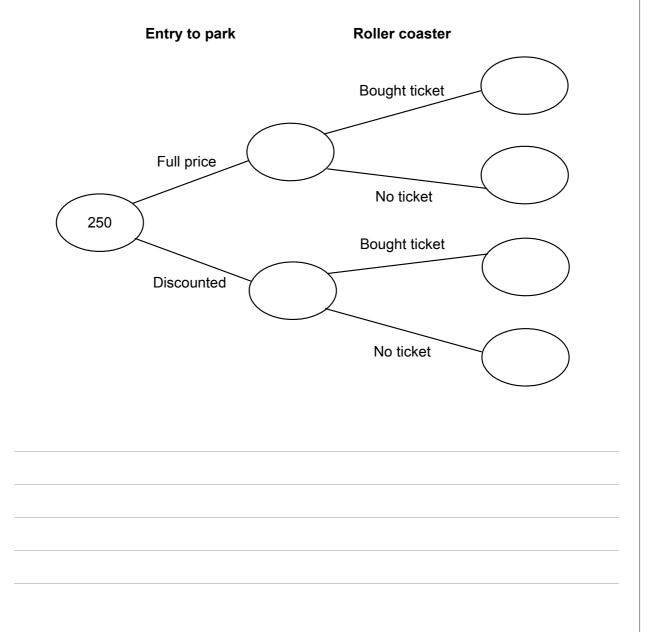
60% of these people paid full price to enter the park.

 $\frac{2}{3}$  of those who paid full price also bought a ticket for the roller coaster.

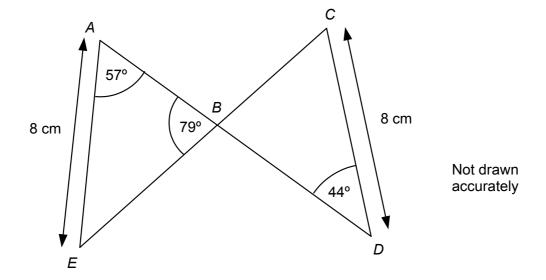
80% of those who bought a ticket for the roller coaster had paid full price to enter the park.

Complete this frequency tree.

[4 marks]



|    |     | e contestant completes the task in less than a minute, they keep all £8000.  r each full minute spent doing the task, the money in the pot decreases by 20%. |
|----|-----|--|
| 22 | (a) | James says   |
|    |     | "If they take longer than 5 minutes they don't win any money."   |
|    |     | Explain why James is not correct. [1 mark]   |
|    |     |  |
| 22 | (b) | Show that a contestant who completes the task in 2 minutes and 21 seconds wins £5120.  |
|    |     | [2 marks]  |
|    |     |  |
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The straight lines AD and CE intersect at the point B.

Use the information on the diagram to prove that triangles ABE and CBD are congruent.

| [3 marks] |
|-----------|
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# **END OF QUESTIONS**